Constrained Superfields and Standard Realization of Nonlinear Supersymmetry

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Abstract

A constrained superfield formalism has been proposed in [10] to analyze the low energy physics related to Goldstinos. We prove that this formalism can be reformulated in the language of standard realization of nonlinear supersymmetry. New relations have been uncovered in the standard realization of nonlinear supersymmetry.

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Associated with spontaneous breaking of global symmetries, there are always massless Nambu-Goldstone (NG) particles. The properties of these NG particles depend on the nature of the broken and unbroken symmetries. In strong interactions, pions are closely related to the spontaneous breaking of chiral symmetry. The low energy physics related to the pions has been systematically analyzed in the framework of nonlinear realization of chiral symmetry (see [1] and the reference therein).

For spontaneous breaking of global supersymmetry (SUSY), one gets a fermionic NG particle, the Goldstino.¹ The low energy physics related to the Goldstino has also been studied in the framework of nonlinear realization of SUSY. Such a framework was first proposed by [2] and most of the study was formalized in the so-called standard realization of nonlinear SUSY [3, 4, 5]. Both superfield [6] and component formalisms [7, 8] have been developed.²

Recently, a new approach has been proposed to address the low energy physics related to Goldstinos [10]. Instead of a manifestly nonlinear realization of SUSY, constrained superfields are used to integrate out heavy components. The Goldstino resides in a (constrained) chiral superfield X_{NL} . The standard superspace technique is retained to write out Lagrangians while the superfields are constrained to include only the light degrees of freedom. In this paper, we will prove that such a procedure can be reformulated in the language of standard realization of nonlinear SUSY. The chiral superfield X_{NL} can be constructed from the Goldstino and a suitable matter field. The constraints on other superfields in [10] can also be rephrased in the language of the standard realization.

In the standard realization of nonlinear SUSY, the Goldstino field and matter fields change as,

$$\delta_{\xi}\tilde{\lambda}_{\alpha} = \frac{\xi_{\alpha}}{\kappa} - i\kappa v_{\xi}^{\mu}\partial_{\mu}\tilde{\lambda}_{\alpha}, \quad \delta_{\xi}\bar{\tilde{\lambda}}_{\dot{\alpha}} = \frac{\bar{\xi}_{\dot{\alpha}}}{\kappa} - i\kappa v_{\xi}^{\mu}\partial_{\mu}\bar{\tilde{\lambda}}_{\dot{\alpha}}$$
 (1)

$$\delta_{\xi}\tilde{\varphi} = -i\kappa v_{\xi}^{\mu}\partial_{\mu}\tilde{\varphi} \tag{2}$$

under a SUSY transformation, respectively. Here $v_{\xi}^{\mu} = \tilde{\lambda} \sigma^{\mu} \bar{\xi} - \xi \sigma^{\mu} \bar{\tilde{\lambda}}$. For discussions related to chiral fields, as in most of this paper, it is more convenient to use the chiral

¹ In the presence of supergravity, the Goldstino becomes part of the massive gravitino. However, if SUSY breaks at a scale much smaller than the Planck scale, the lower energy physics will be dominated by the Goldstino. Depending on the detailed nature of SUSY breaking, Goldstino physics could be of importance at the TeV scale, as to be tested in the coming LHC experiments.

² To reconcile gauge symmetries with SUSY, gauge fields have been assigned a slightly different transformation rule than that in the standard realization [9]. There will be more discussions on this issue at the end of the paper.

version of nonlinear SUSY. The transformations are defined as,

$$\delta_{\xi}\lambda_{\alpha} = \frac{\xi_{\alpha}}{\kappa} - 2i\kappa\lambda\sigma^{\mu}\bar{\xi}\partial_{\mu}\lambda_{\alpha}, \quad \delta_{\xi}\bar{\lambda}_{\dot{\alpha}} = \frac{\bar{\xi}_{\dot{\alpha}}}{\kappa} + 2i\kappa\xi\sigma^{\mu}\bar{\lambda}\partial_{\mu}\bar{\lambda}_{\dot{\alpha}}$$
 (3)

$$\delta_{\xi}\varphi = -2i\kappa\lambda\sigma^{\mu}\bar{\xi}\partial_{\mu}\varphi, \quad \delta_{\xi}\varphi^{c} = 2i\kappa\xi\sigma^{\mu}\bar{\lambda}\partial_{\mu}\varphi^{c}$$

$$\tag{4}$$

They are equivalent and related to the non-chiral one, via,

$$\lambda_{\alpha}(x) = \tilde{\lambda}_{\alpha}(z), \qquad \bar{\lambda}_{\dot{\alpha}}(x) = \bar{\tilde{\lambda}}_{\dot{\alpha}}(z^{*})$$

$$z = x - i\kappa^{2}\tilde{\lambda}(z)\sigma\bar{\tilde{\lambda}}(z), \quad z^{*} = x + i\kappa^{2}\tilde{\lambda}(z^{*})\sigma\bar{\tilde{\lambda}}(z^{*})$$

$$\varphi(x) = \tilde{\varphi}(z), \qquad \varphi^{c}(x) = \tilde{\varphi}(z^{*})$$

$$(5)$$

It started in [10] with the assumption that the Goldstino field resides in a chiral superfield X_{NL} , following the supersymmetry structure and its breaking. It transforms linearly under SUSY transformations:

$$\delta_{\xi} x_{NL} = \sqrt{2} \xi G,
\delta_{\xi} G_{\alpha} = \sqrt{2} \xi_{\alpha} F + i \sqrt{2} (\sigma^{\mu} \bar{\xi})_{\alpha} \partial_{\mu} x_{NL} ,
\delta_{\xi} F = i \sqrt{2} \bar{\xi} \bar{\sigma}^{\mu} \partial_{\mu} G_{\alpha}.$$
(6)

To rid of the scalar component, an operator identity $X_{NL}^2 = 0$ was proposed. This fixes $x_{NL} = G^2/2F$ up to an uninteresting additive constant, and one concludes that

$$X_{NL} = \frac{G^2}{2F} + \sqrt{2\theta}G + \theta^2 F , \qquad (7)$$

where all fields are functions of $y = x + i\theta\sigma\bar{\theta}$. One can easly verify that (7) is consistent with the linear SUSY algebra of (6).

Now we define $\lambda^{NL} = G/\sqrt{2}\kappa F$. It is straightforward to verify that, according to the linear SUSY algebra of (6),

$$\delta_{\xi} \lambda_{\alpha}^{NL} = \frac{\xi_{\alpha}}{\kappa} - 2i\kappa \lambda^{NL} \sigma^{\mu} \bar{\xi} \partial_{\mu} \lambda_{\alpha}^{NL} \tag{8}$$

under SUSY transformations. That is, λ^{NL} transforms in exactly the same way as the Goldstino λ in the chiral version of standard realization under supersymmetry transformations. Naturally, λ^{NL} can be identified as the nonlinear Goldstino field and X_{NL} can be written as

$$X_{NL} = F\Theta^2 \tag{9}$$

where $\Theta = \theta + \kappa \lambda$ is introduced for later convenience.

Actually, the above procedure can be reversed. For an arbitrary chiral superfield $\Phi = \phi + \sqrt{2}\theta\psi + \theta^2 F$, one can always define $\lambda^{\Phi} = \psi/\sqrt{2}\kappa F$. From the transformation rules in (6), one easily gets

$$\delta_{\xi}\lambda_{\alpha}^{\Phi} = \frac{\xi_{\alpha}}{\kappa} - 2i\kappa\lambda^{\Phi}\sigma^{\mu}\bar{\xi}\partial_{\mu}\lambda_{\alpha}^{\Phi} + \frac{i}{\kappa F}(\sigma^{\mu}\bar{\xi})_{\alpha}\partial_{\mu}\left(\phi - \frac{\psi^{2}}{2F}\right)$$
(10)

Demanding λ^{Φ} to transform in the same way as that of λ , one gets $\phi = \psi^2/2F$ up to an additive constant. In such case, one again obtains $\Phi^2 = 0$ as well as $\Phi = F\Theta^2$.

In [6], λ was prompted to a linear superfield by using SUSY transformations in (3),

$$\Lambda(\lambda) = \exp(\theta Q + \bar{\theta}\bar{Q}) \times \lambda$$

Out of Λ and its conjugate $\bar{\Lambda}$, one can construct two possible chiral fields

$$\Phi_2 = -\frac{1}{4}\bar{D}^2\Lambda\Lambda, \quad \Phi_4 = -\frac{1}{4}\bar{D}^2\Lambda\Lambda\bar{\Lambda}\bar{\Lambda}.$$

Direct calculations yield,

$$\Phi_2 = f_2(\lambda)\Theta^2, \quad \Phi_4 = f_4(\lambda)\Theta^2, \tag{11}$$

where f_2 and f_4 are two definite functions of λ and their explicit forms do not concerns us here. f_4 is actually the Akulov-Volkov Lagrangian for the Goldstino [2] up to an overall constant and possible total derivative terms. It is straightforward to verify that f_4/f_2 and F/f_2 transform as matter fields via (4), by using the SUSY algebra of (6). Such relations have not been expected.

It has been well known that Φ_4 satisfies the following constraint [6, 11]

$$\Phi_4 \bar{D}^2 \bar{\Phi}_4 \sim \Phi_4$$

while Φ_2 does not. For long, this constraint was used as the rationale to choose Φ_4 instead of Φ_2 to be the superfield for Goldstino. As one sees now, they differ only by a matter field in the standard realization. In retrospect, this relation is rather easy to understand. Both Φ 's satisfy the same algebraic constraint of X_{NL} , that is, $\Phi_2^2 = \Phi_4^2 = 0$. They must have the same form of factorization.

To recapture, the constrained X_{NL} in [10] can be factorized as follows

$$X_{NL} = F'\Phi_4 = F'f_4(\lambda)\Theta^2 \tag{12}$$

where F' transforms as a nonlinearly realized matter field and Φ_4 is constructed from the nonlinearly realized Goldstino field alone. Obviously, we can reverse the procedure and construct the desired X_{NL} from Goldstino and an appropriate matter field.

One can also use a real superfield to describe the Goldstino [6], $V_4 = \Lambda^2 \bar{\Lambda}^2$. It satisfies the same constraint of X_{NL} , $V_4^2 = 0$. A straightforward calculation reveals a similar simple structure, $V_4 = \tilde{f}_4(\tilde{\lambda})\tilde{\Theta}^2\bar{\tilde{\Theta}}^2$, where $\tilde{\Theta} = \theta + \kappa\tilde{\lambda}$. \tilde{f}_4 is again the Akulov-Volkov Lagrangian for the Goldstino [2] up to an overall constant and possible total derivative terms. Note that the condition $V^2 = 0$ cannot be preserved under a general gauge transformation, if V originates from a gauge superfield. However, for a general real superfield $V = D\theta^2\bar{\theta}^2 + \chi\theta\bar{\theta}^2 + \bar{\chi}\bar{\theta}\theta^2 + \cdots$, one can also define $\lambda^V = \chi/2\kappa D$. From the SUSY transformation rules for a linear real superfield, one finds,

$$\delta_{\xi} \lambda_{\alpha}^{V} = \frac{\xi_{\alpha}}{\kappa} - i(\lambda^{V} \sigma^{\mu} \bar{\xi} - \xi \sigma^{\mu} \bar{\lambda}^{V}) \partial_{\mu} \lambda_{\alpha}^{V} + \frac{i}{D} (\text{total derivatives})$$
 (13)

Demanding the total derivatives to vanish such that λ^V transforms in the same way as that of $\tilde{\lambda}$, one gets $V = D\tilde{\Theta}^2\bar{\tilde{\Theta}}^2$, after some elementary algebra. In this case, it is also easy to check that D/\tilde{f}_4 transforms as a matter field in the standard realization.

When SUSY is broken, some components of superfields will get heavy and need to be integrated out. To rid of the scalar component in a chiral superfield, $Q_{NL} = \phi_q + \sqrt{2}\theta\psi_q + \theta^2 F_q$, [10] suggested to use the constraint,

$$X_{NL}Q_{NL} = 0 (14)$$

From which, one gets

$$\phi_q = \frac{\psi_q G}{F} - \frac{G^2}{2F^2} F_q \tag{15}$$

To rid of the fermionic component in a chiral superfield, $\mathcal{H}_{NL} = H + \sqrt{2}\theta\psi_h + \theta^2 F_h$, [10] suggested to use the constraint,

$$X_{NL}\bar{D}_{\dot{\alpha}}\bar{\mathcal{H}}_{NL} = 0$$
, or equivalently, $X_{NL}\bar{\mathcal{H}}_{NL} = \text{chiral}$ (16)

From which, one gets,

$$\mathcal{H}_{NL} = H + i\sqrt{2}\theta\sigma^{\mu}\left(\frac{\bar{G}}{\bar{F}}\right)\partial_{\mu}H + \theta^{2}\left[-\partial_{\nu}\left(\frac{\bar{G}}{\bar{F}}\right)\bar{\sigma}^{\mu}\sigma^{\nu}\frac{\bar{G}}{\bar{F}}\partial_{\mu}H + \frac{1}{2\bar{F}^{2}}\bar{G}^{2}\partial^{2}H\right]$$
(17)

In the standard realization, nonlinearly realized superfields can be obtained from linear ones via

$$\hat{\Phi} = \exp\left[-\kappa \left(\tilde{\lambda}Q + \bar{\tilde{\lambda}}\bar{Q}\right)\right] \times \Phi \tag{18}$$

Starting with a chiral superfield $\Phi(y,\theta) = \phi(y) + \sqrt{2}\theta\psi(y) + \theta^2 F_{\phi}(y)$ and expressing $\tilde{\lambda}$ in terms of λ via (5), one gets

$$\hat{\Phi}(y,\theta,\lambda) = \hat{\phi}(y,\lambda) + \sqrt{2}\theta\hat{\psi}(y,\lambda) + \theta^2\hat{F}_{\phi}(y,\lambda).$$

The transformation rules are as the following,

$$\delta_{\xi}\hat{\Phi} = -2i\kappa\lambda\sigma^{\mu}\bar{\xi}\partial_{\mu}\hat{\Phi} \tag{19}$$

That is, $\hat{\phi}$, $\hat{\psi}$, and \hat{F} transform independently, each of them can be set to vanish without in conflict with others. Setting $\hat{\phi}(y,\lambda) = 0$ to rid of the scalar component, one reproduces the constraint (15). Setting $\hat{\psi}(y,\lambda) = 0$ to rid of the fermionic component, one does not reproduce (17) exactly. However, one notices by an inspection of (17) that

$$\delta_{\xi} H = 2i\kappa \xi \sigma^{\mu} \bar{\lambda} \partial_{\mu} H \tag{20}$$

which transforms in the same way of φ^c in (4). That is, H transforms as an anti-chiral matter field under SUSY transformations. Actually, it is straightforward to verify that $\mathcal{H}_{NL} = \exp \left[\theta Q + \bar{\theta}\bar{Q}\right] \times H$, by virtue of $\theta Q \times H = 2i\kappa\theta\sigma^{\mu}\bar{\lambda}\partial_{\mu}H$ and $\bar{\theta}\bar{Q} \times H = 0$.

To get a real scalar from a chiral superfield, [10] kept only the real component a of the complex scalar as an independent degree of freedom. The imaginary component b was expressed in terms of a and λ . This was achieved by the constraint

$$X_{NL}\left(\mathcal{A}_{NL} - \bar{\mathcal{A}}_{NL}\right) = 0. \tag{21}$$

Its solution is of the form (17) with $\mathcal{A}_{NL}\big|_{\theta=0}=a+ib$, and b is the following function of a and λ

$$b = \frac{1}{2} \left(\frac{G}{F} \sigma^{\mu} \frac{\bar{G}}{\bar{F}} \right) \partial_{\mu} a - \left(\frac{i}{8} \frac{G^{2}}{F^{2}} \partial_{\nu} \left(\frac{\bar{G}}{\bar{F}} \right) \bar{\sigma}^{\mu} \sigma^{\nu} \frac{\bar{G}}{\bar{F}} \partial_{\mu} a + c.c. \right)$$
$$- \frac{G^{2} \bar{G}^{2}}{32 F^{2} \bar{F}^{2}} \partial_{\mu} \left(\frac{\bar{G}}{\bar{F}} \right) \left(\bar{\sigma}^{\rho} \sigma^{\mu} \bar{\sigma}^{\nu} + \bar{\sigma}^{\mu} \sigma^{\nu} \bar{\sigma}^{\rho} \right) \partial_{\nu} \left(\frac{G}{F} \right) \partial_{\rho} a .$$
 (22)

Since \mathcal{A}_{NL} has the form of (17), a+ib transforms in the same way of φ^c in (4), as an anti-chiral matter field under SUSY transformations. As mentioned at the beginning of the paper, any nonlinearly realized non-chiral matter field $\tilde{\varphi}$ can be converted into an anti-chiral one $\varphi^c = a_{\varphi}^c + ib_{\varphi}^c$ via (5). Here a_{φ}^c and b_{φ}^c are two real fields, as functions of $\tilde{\varphi}$ and λ . If $\tilde{\varphi}$ is a real scalar field, it is straightforward but tedious to check that b_{φ}^c is related to a_{φ}^c via (22). Reversing the procedure, we get one nonlinearly realized

non-chiral real matter field in the non-chiral version from $\mathcal{A}_{NL}\big|_{\theta=0}=a+ib$ by inverting the transformation (5).

For a supersymmetric gauge field

$$V = c + i\theta\omega - i\bar{\theta}\bar{\omega} + \theta^2M + \bar{\theta}^2\bar{M} - \theta\sigma^m\bar{\theta}A_m$$

$$+i\theta^2\bar{\theta}(\bar{\chi} + \frac{i}{2}\bar{\sigma}^m\partial_m\omega) - i\bar{\theta}^2\theta(\chi + \frac{i}{2}\sigma^m\partial_m\bar{\omega}) + \frac{1}{2}\theta^2\bar{\theta}^2(D + \frac{1}{2}\partial^2c)$$

$$(23)$$

the nonlinearly realized version is again obtained via

$$\hat{V} = \exp\left[-\kappa \left(\tilde{\lambda}Q + \bar{\tilde{\lambda}}\bar{Q}\right)\right] \times V \tag{24}$$

All components of \hat{V} transform independently according to (2). In [10], a Wess-Zumino type gauge choice was obtained by imposing the constraint $X_{NL}V_{NL}=0$. Its components solution is

$$c = \frac{\bar{G}\bar{\sigma}^{\mu}G}{2|F|^{2}}A_{\mu} + \frac{i\bar{G}^{2}G\chi}{2\sqrt{2}\bar{F}^{2}F} - \frac{iG^{2}\bar{G}\bar{\chi}}{2\sqrt{2}F^{2}\bar{F}} + \frac{G^{2}\bar{G}^{2}D}{8|F|^{4}} + \dots$$

$$\omega = -i\frac{\bar{G}\bar{\sigma}^{\mu}}{\sqrt{2}\bar{F}}A_{\mu} + \frac{\bar{G}^{2}}{2\bar{F}^{2}}\chi + \dots$$

$$M = i\frac{\bar{G}\bar{\chi}}{\sqrt{2}\bar{F}} - \frac{\bar{G}^{2}}{4\bar{F}^{2}}D + \dots ,$$
(25)

where the ellipses represent terms with more Goldstinos and more derivatives. Interestingly, these expressions can be obtained by demanding $\hat{c} = \hat{\omega} = \hat{M} = 0$, such that \hat{V} is in the Wess-Zumino type gauge.

To rid of the gaugino field χ , it is simpler by working with the field strength superfield

$$W_{\alpha} = -i\chi_{\alpha} + L_{\alpha}^{\beta}\theta_{\beta} + \sigma_{\alpha\dot{\alpha}}^{m}\partial_{m}\bar{\chi}^{\dot{\alpha}}\theta^{2} , \quad L_{\alpha}^{\beta} = \delta_{\alpha}^{\beta}D - \frac{i}{2}(\sigma^{m}\bar{\sigma}^{n})_{\alpha}^{\beta}F_{mn} . \tag{26}$$

The constraint which eliminates the gaugino χ is $X_{NL}W_{\alpha NL}=0$. From this, one has [10]

$$-i\chi_{\alpha} = L_{\alpha}^{\beta} \frac{G_{\beta}}{\sqrt{2}F} - \sigma_{\alpha\dot{\alpha}}^{m} \partial_{m} \bar{\chi}^{\dot{\alpha}} \frac{G^{2}}{2F^{2}}$$
 (27)

This can also be obtained by imposing the condition $\hat{\chi}_{\alpha} = 0$. Here $\hat{\chi}_{\alpha}$ is the first component of $\hat{W}_{\alpha} = \exp\left[-\kappa\left(\tilde{\lambda}Q + \bar{\tilde{\lambda}}\bar{Q}\right)\right] \times W_{\alpha}$.

Finally, we comment on the compatibility between nonlinear SUSY and gauge symmetries. When dealing with non-chiral superfields, such as the vector superfields, the chiral version of nonlinear realization loses much of its virtue. This might be part of the reason

why the constraints on vector superfields in [10] are quite involved. To deal with gauge fields, it could prove to be expedient to work with the non-chiral version.

Working in the Wess-Zumino gauge, one starts with the transformation

$$\delta_{\xi} A_{\mu} = -i\chi \sigma_{\mu} \bar{\xi} + i\xi \sigma_{\mu} \bar{\chi}
\delta_{\xi} \chi_{\alpha} = \sigma^{\mu\nu} \xi_{\alpha} F_{\mu\nu} + i\xi D,
\delta_{\xi} D = -D_{\mu} \chi \sigma^{\mu} \bar{\xi} - \xi \sigma^{\mu} D_{\mu} \bar{\chi}.$$
(28)

where

$$D_{\mu} = \partial_{\mu} - iA_{\mu}$$
 and $F_{\mu\nu} = \partial_{\mu}A_{\nu} - i\partial_{\nu}A_{\mu} - i[A_{\mu}, A_{\nu}]$

From these transformation laws, one can construct a set of four superfields [9]

$$V_{\mu} = \exp(\theta Q + \bar{\theta}\bar{Q}) \times A_{\mu} \tag{29}$$

Out of which, we form four nonlinearly realized superfields

$$\hat{V}_{\mu} = \exp\left[-\kappa(\tilde{\lambda}Q + \bar{\tilde{\lambda}}\bar{Q})\right] \times V_{\mu} = \hat{A}_{\mu} + i\theta\sigma_{\mu}\bar{\hat{\chi}} - i\hat{\chi}\sigma_{\mu}\bar{\theta} + \cdots$$
(30)

We can rid of the feminonic componet by demainding $\hat{\chi} = 0$, which can be used to obtain χ in terms of A_{μ} and D. One may proceed to get the effective Lagrangian via the superspace formalism, with such constraints.

On the other hand, it is straightforward to verify that

$$\delta_{\xi} \hat{A}_{\mu} = -i\kappa v_{\xi}^{\nu} \hat{F}_{\nu\mu} \tag{31}$$

where $\hat{F}_{\mu\nu} = \partial_{\mu}\hat{A}_{\nu} - i\partial_{\nu}\hat{A}_{\mu} - i[\hat{A}_{\mu}, \hat{A}_{\nu}]$. This can be rewritten as

$$\delta_{\xi} \hat{A}_{\mu} = -i\kappa v_{\xi}^{\nu} \partial_{\nu} \hat{A}_{\mu} - i\kappa \partial_{\mu} v_{\xi}^{\nu} \hat{A}_{\nu} + D_{\mu} (i\kappa v_{\xi}^{\nu} \hat{A}_{\nu})$$
(32)

The last term in this expression can be compensated by a gauge transformation of the parameter $-i\kappa v_{\xi}^{\nu}\hat{A}_{\nu}$. Under this combination of SUSY and gauge transformations, one has

$$\delta'_{\xi}\hat{A}_{\mu} = -i\kappa v_{\xi}^{\nu}\partial_{\nu}\hat{A}_{\mu} - i\kappa\partial_{\mu}v_{\xi}^{\nu}\hat{A}_{\nu} \tag{33}$$

One may use $T^{\nu}_{\mu} = \delta^{\nu}_{\mu} - i\kappa^2 \partial_{\mu}\tilde{\lambda}\sigma^{\nu}\bar{\tilde{\lambda}} + i\kappa^2\tilde{\lambda}\sigma^{\nu}\partial_{\mu}\bar{\tilde{\lambda}}$ to define

$$\mathcal{D}_{\mu} = (T^{-1})^{\nu}_{\mu} D_{\nu} = (T^{-1})^{\nu}_{\mu} (\partial_{\nu} - iA_{\nu}) \tag{34}$$

$$\mathcal{F}_{\mu\nu} = (T^{-1})^{\rho}_{\mu} (T^{-1})^{\sigma}_{\nu} (\partial_{\rho} A_{\sigma} - \partial_{\sigma} A_{\rho} - i[A_{\rho}, A_{\sigma}]) \tag{35}$$

Both \mathcal{D}_{μ} and $\mathcal{F}_{\mu\nu}$ transform covariantly under both SUSY and gauge rotation. We can construct SUSY Lagrangians with gauge invariance in the component formalism, by simply making the substitution, $D_{\mu} \to \mathcal{D}_{\mu}$ and $F_{\mu\nu} \to \mathcal{F}_{\mu\nu}$, in ordinary non-SUSY Lagrangians.

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